

TELANGANA RESIDENTIAL EDUCATIONAL INSTITUTIONS RECRUITMENT BOARD TREI-RB

Notations :

- 1.Options shown in green color and with ✓ icon are correct.
- 2.Options shown in red color and with ✗ icon are incorrect.

Question Paper Name :	Mathematics 18thAug 2023 Shift 2
Subject Name :	Mathematics
Creation Date :	2023-08-18 15:20:45
Duration :	120
Total Marks :	100
Display Marks:	Yes
Calculator :	None
Magnifying Glass Required? :	No
Ruler Required? :	No
Eraser Required? :	No
Scratch Pad Required? :	No
Rough Sketch/Notepad Required? :	No
Protractor Required? :	No
Show Watermark on Console? :	Yes
Highlighter :	No
Auto Save on Console?	Yes
Change Font Color :	No
Change Background Color :	No
Change Theme :	No
Help Button :	No
Show Reports :	No
Show Progress Bar :	No

Mathematics

Group Number :	1
Group Id :	594253111
Group Maximum Duration :	0
Group Minimum Duration :	120
Show Attended Group? :	No
Edit Attended Group? :	No
Break time :	0
Group Marks :	100

Is this Group for Examiner? :	No
Examiner permission :	Cant View
Show Progress Bar? :	No

Mathematics

Section Id :	594253127
Section Number :	1
Section type :	Online
Mandatory or Optional :	Mandatory
Number of Questions :	100
Number of Questions to be attempted :	100
Section Marks :	100
Enable Mark as Answered Mark for Review and Clear Response :	Yes
Maximum Instruction Time :	0
Sub-Section Number :	1
Sub-Section Id :	594253165
Question Shuffling Allowed :	Yes
Is Section Default? :	null

Question Number : 1 Question Id : 59425311030 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If a and b are natural numbers such that $5^{a-5} - 5^{b-5} = 624$, then

Options :

1. ✘ $a = 10, b = 6$

2. ✔ $b = 5$ but a cannot be determined

3. ✘ $a = 9, b = 5$

4. ✘ the information is not enough for a and b to be determined

Question Number : 2 Question Id : 59425311031 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of elements in the ring of integers modulo 15 whose square is 1 is

Options :

1. ✘ 4

2. ✘ 3

3. ✘ 2

4. ✔ 1

Question Number : 3 Question Id : 59425311032 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The value of $67^{803} \pmod{15}$ is

Options :

1. ✔ 2

2. ✘ 5

3. ✘ 4

4. ✘ 13

Question Number : 4 Question Id : 59425311033 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$$\sum_{d|120} \phi(d) - 120 =$$

Options :

1. ✘ 0

2. ✓ 3

3. ✗ 5

4. ✗ 10

Question Number : 5 Question Id : 59425311034 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If p is an odd prime and

$(X-1)(X-2)\dots(X-(p-1)) = X^{p-1} + a_1X^{p-2} + a_2X^{p-3} + \dots + a_{p-1}$,
then $a_{p-1} =$

Options :

1. ✗ $1(\text{mod } p)$

2. ✗ $0(\text{mod } p)$

3. ✗ $2(\text{mod } p)$

4. ✓ $-1(\text{mod } p)$

Question Number : 6 Question Id : 59425311035 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Suppose a and b are natural numbers and u, v integers such that

$au + bv = 1$. Then a solution of the congruence $aX \equiv t(\text{mod } b)$ is

Options :

1. ✗ $X = uv$

2. ✗ $X = ut$

3. ✓ $X = vt$

4. ✗ $X = uvt$

Question Number : 7 Question Id : 59425311036 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of integers which are simultaneously congruent to $1 \pmod{3}$, $2 \pmod{5}$, $3 \pmod{7}$ and $4 \pmod{11}$ and which lie between 0 and 2310 are

Options :

1. ✗ 0

2. ✗ 1

3. ✓ 2

4. ✗ 3

Question Number : 8 Question Id : 59425311037 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following statements is **FALSE**?

Options :

1. ✗ Every group of order 55 is cyclic

2. ✓ Every group of order 33 is cyclic

3. ✗ Every group of order 51 is cyclic

4. ✗ Every group of order 35 is cyclic

Question Number : 9 Question Id : 59425311038 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of Sylow 5 subgroups in the permutation group S_5 is

Options :

1. ✘ 7

2. ✘ only one

3. ✘ 5

4. ✔ 6

Question Number : 10 Question Id : 59425311039 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The maximum possible order of an element in S_{10} is

Options :

1. ✘ 10!

2. ✘ 30

3. ✘ 21

4. ✔ 14

Question Number : 11 Question Id : 59425311040 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of possible homomorphisms from a cyclic group of order 8 to a cyclic group of order 6 is

Options :

1. ✘ 1
2. ✘ 2
3. ✘ 3
4. ✔ 4

Question Number : 12 Question Id : 59425311041 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following statements is TRUE?

Options :

1. ✔ The direct product of two cyclic groups must be cyclic
2. ✘ A group of order pq , where p, q are distinct primes, must have a normal Sylow subgroup
3. ✘ A dihedral group of order 10 must be simple
4. ✘ $(\mathbb{R}, +)$ is isomorphic to $(\mathbb{R} \setminus \{0\}, \cdot)$

Question Number : 13 Question Id : 59425311042 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If y is an element in a group and the order of y is 5 and $x \neq e$ is an element in the group such that $xyx^{-1} = x^2$, then the order of x must be

Options :

1. ✘ 8

2. ✘ 16

3. ✘ 25

4. ✔ 31

Question Number : 14 Question Id : 59425311043 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of possible homomorphisms from a dihedral group of order 42 to a group of order 25 is

Options :

1. ✘ 1 only

2. ✘ 3

3. ✘ 5

4. ✔ 7

Question Number : 15 Question Id : 59425311044 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In the alternating group A_4 , the number of subgroups of order 6 is

Options :

1. ✘ 1

2. ✘ 0

3. ✔ 2

4. ✘ 3

Question Number : 16 Question Id : 59425311045 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of conjugacy classes in the permutation group S_5 is

Options :

1. ✘ 6

2. ✔ 8

3. ✘ 10

4. ✘ 7

Question Number : 17 Question Id : 59425311046 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following statements is FALSE?

Options :

1. ✘ There exists an injective homomorphism from any group of order 6 to S_6

2. ✘ In an abelian group G of order n , if m divides n then there must exist a subgroup of order m

3. ✔ A group of order 28 must have a unique Sylow 7 subgroup

4. ✘ A group of order 21 must be cyclic

Question Number : 18 Question Id : 59425311047 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of units in the subring $\mathbb{Z} + \mathbb{Z}i = \{a + bi \mid a, b \in \mathbb{Z}\}$ of the complex numbers is

Options :

1. ✘ 1

2. ✘ 2

3. ✔ 3

4. ✘ 4

Question Number : 19 Question Id : 59425311048 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the statements.

S_1 : The polynomial ring $\mathbb{Z}[X]$ is a principal ideal domain.

S_2 : The polynomial ring $\mathbb{Z}_p[X]$ is a Euclidean domain.

Then

Options :

1. ✘ both S_1 and S_2 are false

2. ✘ S_1 is true but S_2 is false

3. ✔ S_1 is false but S_2 is true

4. ✘ both S_1 and S_2 are true

Question Number : 20 Question Id : 59425311049 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of maximal ideals in the ring \mathbb{Z}_{900} of integers modulo 900 is

Options :

1. ✘ 1
2. ✘ 3
3. ✘ 5
4. ✔ 9

Question Number : 21 Question Id : 59425311050 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the statements.

S_1 : In a commutative ring with 1 prime ideals and maximal ideals are the same.

S_2 : If P is a prime ideal in a ring R with 1, then R/P is an integral domain.

Then

Options :

1. ✔ both S_1 and S_2 are false
2. ✘ S_1 is true but S_2 is false
3. ✘ S_1 is false but S_2 is true
4. ✘ both S_1 and S_2 are true

Question Number : 22 Question Id : 59425311051 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which two of the following four statements are TRUE?

S_1 : The only proper ideal in a field is the zero ideal.

S_2 : In the ring $M_2(\mathbb{Z})$ of 2×2 matrices with integer coefficients the set of matrices of the form $\begin{bmatrix} a & 0 \\ b & 0 \end{bmatrix}$ form a right ideal.

S_3 : All non-zero prime ideals in \mathbb{Z} are also maximal.

S_4 : The ring $C[0, 1]$ of continuous real valued functions on $[0, 1]$ under pointwise addition and multiplication is a ring without unity.

Options :

1. ✘ S_1 and S_4

2. ✔ S_2 and S_3

3. ✘ S_1 and S_3

4. ✘ S_2 and S_4

Question Number : 23 Question Id : 59425311052 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In the ring of Gaussian integers $\mathbb{Z} + \mathbb{Z}i$, which of the following statements is FALSE?

Options :

1. ✘ Every non-zero prime ideal in the ring is maximal

2. ✘ $1 + i$ generates a prime ideal

3. ✔ 7 generates a prime ideal

4. ✘ $5 + 12i$ generates a prime ideal

Question Number : 24 Question Id : 59425311053 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In the ring \mathbb{Z} of integers the ideal generated by 39 and 82 is

Options :

1. ✓ $3\mathbb{Z}$

2. ✗ $41\mathbb{Z}$

3. ✗ \mathbb{Z}

4. ✗ $13\mathbb{Z}$

Question Number : 25 Question Id : 59425311054 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

An example of a ring which is NOT a principal ideal domain is

Options :

1. ✗ \mathbb{Z}

2. ✗ $\mathbb{Z}[X]$

3. ✗ $\mathbb{R}[X]$

4. ✓ \mathbb{Z}_{23}

Question Number : 26 Question Id : 59425311055 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In the direct product ring $\mathbb{Q} \times \mathbb{Z}$, which of the following subsets is NOT a prime ideal?

Options :

1. ✓ $\mathbb{Q} \times 2\mathbb{Z}$
2. ✗ $\{0\} \times \mathbb{Z}$
3. ✗ $\{0\} \times 5\mathbb{Z}$
4. ✗ $\mathbb{Q} \times 5\mathbb{Z}$

Question Number : 27 Question Id : 59425311056 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The number of ring homomorphisms from \mathbb{Z} to \mathbb{Z}_{12} is

Options :

1. ✓ 1
2. ✗ 0
3. ✗ 2
4. ✗ 3

Question Number : 28 Question Id : 59425311057 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

What should x be so that the nullity of the matrix

$$\begin{bmatrix} 1 & -2 & 0 \\ -1 & x & 0 \\ 0 & 0 & 1 \end{bmatrix} \text{ is } 1?$$

Options :

1. ✗ 0

2. ✓ 1

3. ✗ 2

4. ✗ -2

Question Number : 29 Question Id : 59425311058 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In \mathbb{R}^3 , which of the following vectors is not in the space spanned by the vectors $(1,0,0)$ and $(1,1,1)$?

Options :

1. ✓ $(3,2,2)$

2. ✗ $(2,2.5,2.5)$

3. ✗ $(1,1,0)$

4. ✗ $(5,7,7)$

Question Number : 30 Question Id : 59425311059 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The rank and nullity of the matrix $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 2 & 2 & 2 & 2 \\ 3 & 3 & 3 & 3 \\ 4 & 4 & 4 & 4 \end{bmatrix}$ are respectively

Options :

1. ✗ 1 and 2

2. ✘ 1 and 3

3. ✘ 2 and 2

4. ✔ 3 and 1

Question Number : 31 Question Id : 59425311060 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The index and signature of the quadratic form

$-7X_1^2 + 3X_2^2 - 4X_3^2 + 5X_4^2 + 6X_5^2$
are respectively

Options :

1. ✔ 1 and 3

2. ✘ 90 and 28

3. ✘ -28 and 90

4. ✘ 3 and 1

Question Number : 32 Question Id : 59425311061 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In \mathbb{R}^5 , the dimension of the subspace generated by the vectors

$e_1 + e_2, e_2 + e_3, e_3 + e_4, e_4 + e_5$ (e_i is the vector with 1 in the i th place and zeroes everywhere else) is

Options :

1. ✘ 1

2. ✘ 2

3. ✓ 3

4. ✗ 4

Question Number : 33 Question Id : 59425311062 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The characteristic polynomial of the matrix $\begin{bmatrix} 1 & i \\ 1 & -i \end{bmatrix}$ is

Options :

1. ✗ $X^2 - (1 - i)X - 2i$

2. ✓ $X^2 + (1 - i)X + 2i$

3. ✗ $X^2 - (1 - i)X + 2i$

4. ✗ $X^2 + (1 - i)X - 2i$

Question Number : 34 Question Id : 59425311063 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the statements.

S_1 : If the characteristic polynomial of a $n \times n$ complex matrix is of degree 7, then $n = 7$.

S_2 : If an $n \times n$ complex matrix has four distinct eigenvalues then $n = 4$.

Then

Options :

1. ✓ both S_1 and S_2 must be false

2. ✗ S_1 is true but S_2 is false

3. ✘ S_1 is false but S_2 is true

4. ✘ both S_1 and S_2 are true

Question Number : 35 Question Id : 59425311064 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If a 3×3 matrix M has eigenvalues $1, 1, -2$, then the trace of M^5 is

Options :

1. ✘ 0

2. ✘ 6

3. ✘ -30

4. ✔ 32

Question Number : 36 Question Id : 59425311065 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The quadratic form given by $X_1^2 + 2X_1X_2 + X_3^2$ is

Options :

1. ✘ positive definite

2. ✔ negative definite

3. ✘ positive semi-definite

4. ✘ indefinite

Question Number : 37 Question Id : 59425311066 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

In \mathbb{R}^3 , let $v_1 = (1, 2, -1)$, $v_2 = (-1, 3, 1)$. Then which one of the following vectors v_3 is such that $\{v_1, v_2, v_3\}$ is a basis of \mathbb{R}^3 ?

Options :

1. ✘ $(2, 79, -2)$

2. ✘ $(0, 30, 0)$

3. ✘ $(-2, -1, 2)$

4. ✔ $(3, 17, 3)$

Question Number : 38 Question Id : 59425311067 Question Type : MCQ Option Shuffling : Yes Is

Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $A = \begin{bmatrix} \bar{4} & \bar{2} \\ \bar{1} & \bar{3} \end{bmatrix} \in M_2(\mathbb{Z}_7)$, where \mathbb{Z}_7 is the field of 7 elements. Then the additive and multiplicative orders of A are respectively

Options :

1. ✘ 3 and 4

2. ✘ 7 and 4

3. ✘ 4 and 7

4. ✔ 7 and 6

Question Number : 39 Question Id : 59425311068 Question Type : MCQ Option Shuffling : Yes Is

Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following statements is true about complex $n \times n$ matrices?

Options :

1. ✘ All non-singular matrices are diagonalizable
2. ✔ A matrix is diagonalizable if and only if its eigenvalues are distinct
3. ✘ A matrix is diagonalizable if it has n distinct eigenvalues
4. ✘ A matrix is diagonalizable if it has a single eigenvalue

Question Number : 40 Question Id : 59425311069 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$ is given by $T((a, b, c)) = (a - b + c, a + b - c, -a + b + c)$, $a, b, c \in \mathbb{R}$. Then the rank and nullity of T are respectively

Options :

1. ✘ 2 and 1
2. ✘ 1 and 2
3. ✔ 0 and 3
4. ✘ 3 and 0

Question Number : 41 Question Id : 59425311070 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let M_3 denote the vector space of all 3×3 matrices with complex entries over the field \mathbb{R} and $V = \{A \in M_3 \mid A \text{ is a skew-Hermitian matrix}\}$.

Then the dimension of $\frac{M_3}{V}$ over the field \mathbb{R} is

Options :

1. ✘ 6
2. ✘ 3
3. ✘ 9
4. ✔ 12

Question Number : 42 Question Id : 59425311071 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0.25

Which of the following is a finite dimensional vector space?

Options :

1. ✔ vector space \mathbb{R} over \mathbb{Q}
2. ✘ vector space \mathbb{C} over \mathbb{Q}
3. ✘ vector space \mathbb{C} over \mathbb{R}
4. ✘ vector space V_2 over \mathbb{R} , where $V_2 = \{f : (0, 1) \rightarrow \mathbb{R} \mid f \text{ is twice differentiable}\}$

Question Number : 43 Question Id : 59425311072 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0.25

Consider the vector space \mathbb{R}^5 over the field \mathbb{R} . Let $|A|$ denote the number of elements in the set A . Then, which of the following statements is FALSE?

Options :

1. ✘ There exists a linearly independent set $A \subset \mathbb{R}^5$ with $|A| = 3$

2. ✘ There exists $A \subset \mathbb{R}^5$ such that $|A| = 3$ and A spans \mathbb{R}^5

3. ✘ There exists $A \subset \mathbb{R}^5$ such that $|A| = 10$ and A spans \mathbb{R}^5

4. ✔ If $A \subset \mathbb{R}^5$, $|A| = 10$, the A is linearly dependent

Question Number : 44 Question Id : 59425311073 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let (V, \langle, \rangle) be a finite dimensional inner product space. Consider the following statements.

S_1 : If $x_i \perp x_j, \forall 1 \leq i, j \leq n, i \neq j$, then $\|\sum_{i=1}^n x_i\|^2 = \sum_{i=1}^n \|x_i\|^2$

S_2 : If V^* denotes the dual of V , then V is isomorphic to V^* .

Then

Options :

1. ✘ S_1 is true, S_2 is false

2. ✘ S_2 is true, S_1 is false

3. ✔ S_1 is true, S_2 is true

4. ✘ S_1 is false, S_2 is false

Question Number : 45 Question Id : 59425311074 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following norms on \mathbb{R}^n is given by an inner product?

Options :

1. ✘ $\|\bar{x}\| = \sum_{i=1}^n |x_i|, \forall \bar{x} = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$

2. ✔ $\|\bar{x}\| = \max_{1 \leq i \leq n} |x_i|, \forall \bar{x} = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$

3. ✘ $\|\bar{x}\| = \left(\sum_{i=1}^n |x_i|^2 \right)^{\frac{1}{2}}, \forall \bar{x} = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$

4. ✘ $\|\bar{x}\| = \left(\sum_{i=1}^n |x_i|^3 \right)^{\frac{1}{3}}, \forall \bar{x} = (x_1, x_2, \dots, x_n) \in \mathbb{R}^n$

Question Number : 46 Question Id : 59425311075 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let (V, \langle, \rangle) be a finite dimensional inner product space. Consider

S_1 : For every proper subspace W of V , \exists a unit vector $\bar{v} \in V$ such that $\bar{v} \in W^\perp$.

S_2 : Let W_1, W_2 be two subspaces of V . Then $W_1 \cap W_2 = \{0\}$ if and only if $W_1 \perp W_2$.

Then

Options :

1. ✘ S_1 is true and S_2 is false

2. ✘ S_2 is true and S_1 is false

3. ✘ S_1 is true and S_2 is true

4. ✔ S_1 is false and S_2 is false

Question Number : 47 Question Id : 59425311076 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following is true for sequences in \mathbb{R} ?

Options :

1. ✘ Every monotonic sequence has a convergent subsequence
2. ✘ Every absolutely convergent sequence is convergent
3. ✔ Every bounded sequence has an absolutely convergent subsequence
4. ✘ Every convergent sequence is monotonic

Question Number : 48 Question Id : 59425311077 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following is FALSE?

Options :

1. ✔ Sums and products of irrational numbers are always irrational
2. ✘ Every irrational number is the limit of suitable convergent sequence of rational numbers
3. ✘ There are uncountably many irrational numbers between any two distinct rational numbers
4. ✘ There is a sequence (a_n) , where each a_n is irrational and $\sum_{n=1}^{\infty} a_n$ is a rational number

Question Number : 49 Question Id : 59425311078 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following statements is FALSE?

Options :

1. ✘ $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$ is convergent

2. ✘ $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$ is absolutely convergent

3. ✔ $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^2}$ is absolutely convergent

4. ✘ $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^{\frac{3}{2}}}$ is convergent

Question Number : 50 Question Id : 59425311079 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $\sum_{n=1}^{\infty} c_n$ be the Cauchy product of $\sum_{n=1}^{\infty} a_n$ and $\sum_{n=1}^{\infty} b_n$. Assume that $\sum_{n=1}^{\infty} b_n$ converges. Then which of the following is FALSE?

Options :

1. ✘ If $\sum_{n=1}^{\infty} a_n$ converges absolutely, then $\sum_{n=1}^{\infty} a_n^2$ converges

2. ✘ If $\sum_{n=1}^{\infty} a_n$ converges absolutely, then $\left(\sum_{n=1}^{\infty} a_n\right)\left(\sum_{n=1}^{\infty} b_n\right) = \sum_{n=1}^{\infty} c_n$

3. ✘ If both $\sum_{n=1}^{\infty} a_n$, $\sum_{n=1}^{\infty} c_n$ converge, then $\left(\sum_{n=1}^{\infty} a_n\right)\left(\sum_{n=1}^{\infty} b_n\right) = \sum_{n=1}^{\infty} c_n$

4. ✓ If $\sum_{n=1}^{\infty} a_n$ converges, then $\sum_{n=1}^{\infty} c_n$ converges

Question Number : 51 Question Id : 59425311080 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following sequences does not converge to e ?

Options :

1. ✗ (x_n) , where $x_n = \left(1 + \frac{1}{n}\right)^n, n \in \mathbb{N}$

2. ✓ (x_n) , where $x_n = \left(1 - \frac{1}{n}\right)^n, n \in \mathbb{N}$

3. ✗ (x_n) , where $x_n = \sum_{k=0}^{2n} \frac{1}{k!}, n \in \mathbb{N}$

4. ✗ (x_n) , where $x_n = \left(1 + \frac{1}{2n+1}\right)^{2n}, n \in \mathbb{N}$

Question Number : 52 Question Id : 59425311081 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$\lim_{n \rightarrow \infty} \sqrt{n} (\sqrt{n+1} - \sqrt{n}) =$

Options :

1. ✓ 1

2. ✗ $\frac{1}{2}$

3. ✘ 0

4. ✘ ∞

Question Number : 53 Question Id : 59425311082 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The function $f : \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = e^x$, $x \in \mathbb{R}$, is

Options :

1. ✔ one - one

2. ✘ onto

3. ✘ one - one and onto

4. ✘ neither one - one nor onto

Question Number : 54 Question Id : 59425311083 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a continuous function, $a, b \in \mathbb{R}$, and $a < b$. Then the set $f([a, b])$ is of the form

Options :

1. ✘ (c, d) , for some $c, d \in \mathbb{R}$

2. ✘ $\bigcup_{i \in \mathbb{N}} (c_i, d_i)$, for some $c_i, d_i \in \mathbb{R}$, $i \in \mathbb{N}$

3. ✘ $[c, d]$, for some $c, d \in \mathbb{R}$

4. ✓ $\bigcup_{i \in \mathbb{N}} [c_i, d_i]$, for some $c_i, d_i \in \mathbb{R}, i \in \mathbb{N}$

Question Number : 55 Question Id : 59425311084 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $f : [1, \infty) \rightarrow \mathbb{R}$ be a continuous function. Which of the following statements is true?

Options :

1. ✓ If f is bounded, then f is uniformly continuous
2. ✗ If f is unbounded, then f is NOT uniformly continuous
3. ✗ If $\lim_{x \rightarrow \infty} f(x)$ exists in \mathbb{R} , then f is uniformly continuous
4. ✗ If f is monotonic, then f is uniformly continuous

Question Number : 56 Question Id : 59425311085 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider $f : \mathbb{R} \rightarrow [-1, 1]$, given by $f(x) = \sin x$. Which of the following statements need NOT be true?

Options :

1. ✗ If D is dense in \mathbb{R} , then $f(D)$ is dense in $[-1, 1]$
2. ✗ If A is closed in \mathbb{R} , then $f(A)$ is closed in $[-1, 1]$
3. ✓ If U is open in $[-1, 1]$, then $f^{-1}(U)$ is open in \mathbb{R}
4. ✗ If A is closed in $[-1, 1]$, then $f^{-1}(A)$ is closed in \mathbb{R}

Question Number : 57 Question Id : 59425311086 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $f : (a, b) \rightarrow \mathbb{R}$ is a differentiable function, then

Options :

1. ✘ f is uniformly continuous
2. ✘ f can be extended continuously to $[a, b]$
3. ✔ f' is continuous on (a, b)
4. ✘ f' has the intermediate value property

Question Number : 58 Question Id : 59425311087 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{1}{n+k} =$$

Options :

1. ✘ $\log 2$
2. ✘ $\log 4$
3. ✘ $\log 6$
4. ✔ $\log 8$

Question Number : 59 Question Id : 59425311088 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{1}{n} e^{\frac{k}{n}} =$$

Options :

1. ✘ e
2. ✔ $e + 1$
3. ✘ $e - 1$
4. ✘ 0

Question Number : 60 Question Id : 59425311089 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following is complete with usual metric?

Options :

1. ✔ $\mathbb{Q} \times (\mathbb{R} \setminus \mathbb{Q})$
2. ✘ $\mathbb{Q} \times \mathbb{C}$
3. ✘ \mathbb{R}^{2023}
4. ✘ $\{(x, y) \in \mathbb{R}^2 / x^2 + y^2 < 1\}$

Question Number : 61 Question Id : 59425311090 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

For $n \in \mathbb{N}$, consider the metric spaces (\mathbb{R}^n, d_2) , (\mathbb{R}^n, D) ,

$$\text{where } d_2(x, y) = \sqrt{\sum_{i=1}^n |x_i - y_i|^2}, \quad D(x, y) = \begin{cases} 1, & x \neq y, \\ 0, & x = y, \end{cases} \quad \forall x, y \in \mathbb{R}^n.$$

Which of the following functions is discontinuous?

Options :

1. ✘ $f : (\mathbb{R}, D) \rightarrow (\mathbb{R}, d_2), f(x) = x, \forall x \in \mathbb{R}$

2. ✘ Fix $y \in \mathbb{R}^n, f : (\mathbb{R}^n, d_2) \rightarrow (\mathbb{R}, d_2), f(x) = y \cdot x, \forall x \in \mathbb{R}^n$

3. ✔ $f : (\mathbb{R}^n, d_2) \rightarrow (\mathbb{R}^n, d_2), f(x) = \begin{cases} x, & \text{if } d_2(0, x) \leq 1, \\ \frac{x}{(d_2(0, x))^2}, & \text{if } d_2(0, x) > 1 \end{cases}$

4. ✘ $f : (\mathbb{R}, d_2) \rightarrow (\mathbb{R}, D), f(x) = x, \forall x \in \mathbb{R}$

Question Number : 62 Question Id : 59425311091 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the metric spaces $(C[0, 1], d_\infty)$, (\mathbb{R}, d_2) , $([1, \infty), d_2)$, where $C[0, 1]$ is the set of all real valued continuous functions from $[0, 1]$,
 $d_\infty(f, g) = \sup_{x \in [0, 1]} |f(x) - g(x)|, \forall f, g \in C[0, 1], d_2(x, y) = |x - y|,$

$\forall x, y \in \mathbb{R}$. Consider the functions defined by $T : C[0, 1] \rightarrow \mathbb{R}$,

$Tf = f(0)$, and $f : [1, \infty) \rightarrow \mathbb{R}, f(x) = \frac{1}{x^5}$. Then

Options :

1. ✘ both f and T are uniformly continuous

2. ✔ f is uniformly continuous but T is not uniformly continuous

3. ✘ T is uniformly continuous but f is not uniformly continuous

4. ✘ both f and T are not uniformly continuous

Question Number : 63 Question Id : 59425311092 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let (X, d) be a compact metric space with infinite number of elements.
Which of the following is NOT true?

Options :

1. ✘ X is complete

2. ✘ X is closed and bounded

3. ✔ (3) There exists an infinite set $S \subset X$ such that every element in S is isolated

4. ✘ X is totally bounded

Question Number : 64 Question Id : 59425311093 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following subsets of \mathbb{R}^2 with Euclidean metric is connected?

Options :

1. ✔ $\{(x, y) \mid x \neq 0\}$

2. ✘ $\{(x, y) \mid x \neq 0\} \cup \{(0, 0)\}$

3. ✘ $\{(x, y) \mid (x^2 + y^2 - 1)(x^2 + y^2 - 2) = 0\}$

4. ✘ $\{(x, y) \mid 2x + 3y = \pm 1\}$

Question Number : 65 Question Id : 59425311094 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let τ_u be the usual topology on \mathbb{R} . Suppose $f : (\mathbb{R}, \tau_u) \rightarrow (\mathbb{R}, \tau_u)$, $f(x) = x^2 + e^x$ and $A = f^{-1}((-2, 5])$. Then A is

Options :

1. ✘ closed but not open
2. ✘ open but not closed
3. ✘ neither closed nor open
4. ✔ both closed and open

Question Number : 66 Question Id : 59425311095 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $B_1 = \{A \subsetneq \mathbb{R} \mid 0 \in A\}$, $B_2 = \{A \subset \mathbb{R} \mid 0 \notin A\} \cup \mathbb{R}$, then

Options :

1. ✘ B_1 is a basis of some topology on \mathbb{R} but B_2 is not so
2. ✘ B_2 is a basis of some topology on \mathbb{R} but B_1 is not so
3. ✔ B_1 and B_2 are bases of some topologies on \mathbb{R}
4. ✘ neither B_1 nor B_2 is a basis of any topology on \mathbb{R}

Question Number : 67 Question Id : 59425311096 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If τ_1 and τ_2 are topologies with bases B_1, B_2 respectively, where $B_1 = \{(a, b) \mid a < b, a, b \in \mathbb{Q}\}$, $B_2 = \{(a, b) \mid a < b, a, b \in \mathbb{R}\}$, then

Options :

1. ✘ $\tau_1 \subset \tau_2$
2. ✘ $\tau_2 \subset \tau_1$
3. ✔ $\tau_1 = \tau_2$
4. ✘ τ_1, τ_2 are not comparable

Question Number : 68 Question Id : 59425311097 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider \mathbb{R} with cofinite topology τ . Then $\{l \mid (\frac{1}{n}) \rightarrow l \text{ in } (\mathbb{R}, \tau)\} =$

Options :

1. ✘ $\{0\}$
2. ✘ $\{\frac{1}{n} \mid n \in \mathbb{N}\} \cup \{0\}$
3. ✘ \mathbb{R}
4. ✔ $(\mathbb{R} \setminus \{\frac{1}{n} \mid n \in \mathbb{N}\}) \cup \{0\}$

Question Number : 69 Question Id : 59425311098 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$$\oint_{|z-2|=4} \frac{dz}{z-2} =$$

Options :

1. ✘ $2\pi i$

2. ✓ 1

3. ✗ 4π

4. ✗ i

Question Number : 70 Question Id : 59425311099 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $f(x + iy) = x^3 - y^3, \forall x, y \in \mathbb{R}$, then

Options :

1. ✗ f satisfies the Cauchy-Riemann equations in \mathbb{C}

2. ✗ f is entire

3. ✓ f is differentiable in $\mathbb{C} \setminus \{0\}$

4. ✗ f is differentiable only at $z = 0$

Question Number : 71 Question Id : 59425311100 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the following statements.

S_1 : There exists a non-constant entire function f such that $|f(z)| > 10, \forall z \in \mathbb{C}$.

S_2 : There exists a non-constant entire function f such that $|f(z)| < 10, \forall z \in \mathbb{C}$.

Then

Options :

1. ✗ S_1 is true and S_2 is false.

2. ✓ S_2 is true and S_1 is false

3. ✗ S_1 is true and S_2 is true

4. ✗ S_1 is false and S_2 is false

Question Number : 72 Question Id : 59425311101 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

$$\oint_{|z|=\pi} \pi \cot(\pi z) dz =$$

Options :

1. ✗ $14\pi i$

2. ✗ 14π

3. ✗ π^2

4. ✓ $14\pi^2$

Question Number : 73 Question Id : 59425311102 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The largest region of convergence of $\sum_{n=1}^{\infty} (-1)^{n-1} \frac{z^{2n-1}}{(2n-1)!}$ is

Options :

1. ✗ $\{z / |z| < 1\}$

2. ✗ $\{z / |z| < 1\} \cup \{x / x \in \mathbb{R}\}$

3. ✘ $\{z/ |z| \leq 1\}$

4. ✔ C

Question Number : 74 Question Id : 59425311103 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The Laurent series of $\frac{z}{(z-1)(2-z)}$ in $|z| < 1$ is

Options :

1. ✘ $-\frac{1}{2}z - \frac{3}{4}z^2 - \frac{7}{8}z^3 - \dots$

2. ✘ $-\frac{1}{2}z + \frac{3}{4}z^2 - \frac{7}{8}z^3 - \dots$

3. ✘ $-\frac{1}{2}z - \frac{3}{4}z^2 + \frac{7}{8}z^3 - \dots$

4. ✔ $-\frac{1}{2}z + \frac{3}{4}z^2 + \frac{7}{8}z^3 + \dots$

Question Number : 75 Question Id : 59425311104 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If the radius of convergence of $\sum_{n=0}^{\infty} a_n z^n$ is $r > 0$, then which of the following series has the same radius of convergence?

Options :

1. ✘ $\sum_{n=0}^{\infty} 3^n a_n z^n$

2. ✘ $\sum_{n=0}^{\infty} z^n$

3. ✘ $\sum_{n=0}^{\infty} r^n z^n$

4. ✔ $\sum_{n=0}^{\infty} n^2 a_n z^n$

Question Number : 76 Question Id : 59425311105 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $D_1 = \{z \in \mathbb{C} / |z| < 1\}$, $f : D_1 \rightarrow D_1$ be analytic. If $f(0) = 0$, $f(\frac{1}{2}) = -\frac{1}{2}$, then $f(\frac{1+i}{2})$ is

Options :

1. ✘ $-\frac{1}{2}(1+i)$

2. ✔ $\frac{1}{2}(1-i)$

3. ✘ $\frac{1}{2}(-1+i)$

4. ✘ not uniquely determined using the given data.

Question Number : 77 Question Id : 59425311106 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Consider the following statements.

S_1 : If $\Omega \subset \mathbb{C}$ is open, $f : \bar{\Omega} \rightarrow \mathbb{C}$ is continuous, f is analytic on Ω , then $\sup_{z \in \partial\Omega} |f(z)| = \sup_{z \in \Omega} |f(z)|$, where $\partial\Omega$ is the boundary of Ω .

S_2 : Let $D_1 = \{z \in \mathbb{C} / |z| < 1\}$, $f : \bar{D}_1 \rightarrow \mathbb{C}$ be continuous and f be analytic on D_1 . If $\min_{\partial\Omega} |f(z)| = 1$, $\max_{\partial\Omega} |f(z)| = 3$ then $1 \leq |f(z)| \leq 3$, $\forall z \in \Omega$.

Then

Options :

1. ✘ S_1 is true, S_2 is false
2. ✔ S_2 is true, S_1 is false
3. ✘ both S_1 and S_2 are true
4. ✘ S_1 is false and S_2 is false

Question Number : 78 Question Id : 59425311107 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If the order and degree of the ordinary differential equation $(y''(x))^3 + (y'(x))^2 + y^2(x) = f(x)$ are p and q , respectively, then $(p, q) =$

Options :

1. ✘ (1, 2)
2. ✘ (2, 3)
3. ✘ (3, 2)
4. ✔ (2, 2)

Question Number : 79 Question Id : 59425311108 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If y is the solution of $y' = 1 + y^2$, $y(0) = 0$, then $y\left(\frac{\pi}{4}\right) =$

Options :

1. ✘ 0

2. ✘ 1

3. ✔ $\sqrt{3}$

4. ✘ 3

Question Number : 80 Question Id : 59425311109 Question Type : MCQ Option Shuffling : Yes Is

Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $y'(x) + y(x) \tan x = \cos x$, $y(0) = 0$ then $y(\pi) =$

Options :

1. ✔ π

2. ✘ 2π

3. ✘ $-\pi$

4. ✘ -2π

Question Number : 81 Question Id : 59425311110 Question Type : MCQ Option Shuffling : Yes Is

Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum

Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Which of the following differential equations is NOT exact?

Options :

1. ✘ $\frac{y}{x^2 + y^2}dx - \frac{x}{x^2 + y^2}dy = 0$

2. ✘ $\frac{1}{x}dx - \frac{1}{y}dy = 0$

3. ✘ $ydx - xdy = 0$

4. ✔ $\frac{1}{y}dx - \frac{x}{y^2}dy = 0$

Question Number : 82 Question Id : 59425311111 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The solution of the differential equation $y(x) = xy'(x) + \sqrt{4 + (y'(x))^2}$ is

Options :

1. ✘ $(y - cx)^2 - 4 - c^2 = 0$, where $c \in \mathbb{R}$ is arbitrary

2. ✘ $(y - cx)^2 + 4c^2 = 0$, where $c \in \mathbb{R}$ is arbitrary

3. ✔ $(y - cx)^2 - c^2 = 0$, where $c \in \mathbb{R}$ is arbitrary

4. ✘ $(y - cx)^2 - 4c^2 = 0$, where $c \in \mathbb{R}$ is arbitrary

Question Number : 83 Question Id : 59425311112 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

An integrating factor for $(x + 1)y'(x) - y(x) = (x + 1)^2 e^{3x}$ is

Options :

1. ✘ $x + 1$

2. ✔ $\frac{1}{(x + 1)^2}$

3. ✘ $\frac{1}{x + 1}$

4. ✘ $(x - 1)^2$

Question Number : 84 Question Id : 59425311113 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $y = x$ is a solution of the differential equation $x^2 \frac{d^2y}{dx^2} + 2x \frac{dy}{dx} - 2y = 0$, then which of the following is another solution?

Options :

1. ✘ x^2

2. ✘ x^{-2}

3. ✔ $x \log x$

4. ✘ xe^x

Question Number : 85 Question Id : 59425311114 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$. Then the partial differential equations $f(x, y, z, p, q) = 0$ and $g(x, y, z, p, q) = 0$ are said to be compatible if

Options :

1. ✓ every solution of $f(x, y, z, p, q) = 0$ is a solution of $g(x, y, z, p, q) = 0$
2. ✗ every solution of $g(x, y, z, p, q) = 0$ is a solution of $f(x, y, z, p, q) = 0$
3. ✗ $f(x, y, z, p, q) = 0$ and $g(x, y, z, p, q) = 0$ have one parameter family of common solutions
4. ✗ $f(x, y, z, p, q) = 0$ and $g(x, y, z, p, q) = 0$ have a unique common solution

Question Number : 86 Question Id : 59425311115 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Let $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$. Then which of the following is a complete integral of $x^2 p^2 + y^2 q^2 = 4$?

Options :

1. ✗ $z = \sqrt{4 - a^2} \log x + a \log y$, where $a \in \mathbb{R}$, $|a| < 2$
2. ✗ $z = \sqrt{4 - a^2} \log y + a \log x + b$, where $a, b \in \mathbb{R}$, $|a| < 2$
3. ✓ $z = a \log x + b \log y$, where $a, b \in \mathbb{R}$
4. ✗ $z = \sqrt{4 - a^2} + a \log x + a$, where $a \in \mathbb{R}$, $|a| < 2$

Question Number : 87 Question Id : 59425311116 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The second order partial differential equation $\frac{\partial^2 u}{\partial x^2} + x \frac{\partial^2 u}{\partial y^2} = x^2 + y^2$ is

Options :

1. ✘ hyperbolic for $x < 0$
2. ✘ hyperbolic for $x > 0$
3. ✘ elliptic for $x < 0$
4. ✔ parabolic for $x > 0$

Question Number : 88 Question Id : 59425311117 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The general solution of $\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial x \partial y} - 6 \frac{\partial^2 z}{\partial y^2} = 0$ is

Options :

1. ✘ $f_1(y + 3x) + f_2(y + 2x)$, where f_1 and f_2 are arbitrary C^2 functions
2. ✘ $f_1(y - 3x) + f_2(y - 2x)$, where f_1 and f_2 are arbitrary C^2 functions
3. ✔ $f_1(y + 3x) + f_2(y - 2x)$, where f_1 and f_2 are arbitrary C^2 functions
4. ✘ $f_1(y - 3x) + f_2(y + 2x)$, where f_1 and f_2 are arbitrary C^2 functions

Question Number : 89 Question Id : 59425311118 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

A particular integral of $\frac{\partial^2 z}{\partial x^2} - 4 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = \cos(x - 2y)$ is

Options :

1. ✘ $\frac{-\cos(x - 2y)}{13}$

2. ✘ $\frac{\cos(x - 2y)}{13}$

3. ✔ $\frac{\cos(2y - x)}{13}$

4. ✘ $\frac{-\cos(2y - x)}{13}$

Question Number : 90 Question Id : 59425311119 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

If $u(x, t)$ is a solution of $\frac{\partial^2 u}{\partial x^2} - 9\frac{\partial^2 u}{\partial t^2} = 0$, with $u(x, 0) = 0$, $\frac{\partial u}{\partial t}(x, 0) = x$, $0 \leq x \leq \infty$, then $u(2, 1) =$

Options :

1. ✘ 2

2. ✘ 4

3. ✘ 6

4. ✔ 8

Question Number : 91 Question Id : 59425311120 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Direction ratios of the line $x + y + z = 0, x + y = 0$ are

Options :

1. ✘ $(1, 1, 0)$
2. ✔ $(1, -1, 0)$
3. ✘ $(-1, -1, -1)$
4. ✘ $(-1, 1, -1)$

Question Number : 92 Question Id : 59425311121 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The equation of the plane parallel to $2x + 3y + 7z = 10$, and passing through $(0, 1, -1)$ is

Options :

1. ✘ $2x + 3y + 7z = 4$
2. ✘ $2x + 3y + 7z + 4 = 0$
3. ✘ $2x + 3y + 3z = 3$
4. ✔ $2x + 3y + 7z + 3 = 0$

Question Number : 93 Question Id : 59425311122 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The distance between $(1, 1, 1)$ and the plane $x + 2y + 2z = 6$ is

Options :

1. ✔ 3
2. ✘ 1

3. ✘ $\frac{1}{3}$

4. ✘ $\frac{1}{\sqrt{3}}$

Question Number : 94 Question Id : 59425311123 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The equation of the line through $(1, 2, 3)$ and orthogonal to $x + 2y + 3z = 10$ is

Options :

1. ✘ $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{3}$

2. ✔ $\frac{x-1}{3} = \frac{y-2}{2} = \frac{z-3}{1}$

3. ✘ $\frac{x-1}{1} = \frac{y-2}{3} = \frac{z-3}{2}$

4. ✘ $\frac{x-1}{2} = \frac{y-2}{1} = \frac{z-3}{3}$

Question Number : 95 Question Id : 59425311124 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

Suppose S is a sphere passing through $P(2, 2, 2), Q(0, 0, 0)$. If the length of \overline{PQ} is the same as the diameter of S , then the equation of S is

Options :

1. ✘ $x^2 + y^2 + z^2 + 2x + 2y + 2z = 0$

2. ✓ $x^2 + y^2 + z^2 - 2x - 2y - 2z = 0$

3. ✗ $x^2 + y^2 + z^2 - 4x - 4y - 4z = 0$

4. ✗ $x^2 + y^2 + z^2 + 4x + 4y + 4z = 0$

Question Number : 96 Question Id : 59425311125 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The equation of the tangent plane to the sphere $x^2 + y^2 + z^2 - 4x - 4y - 4z + 3 = 0$ at $(1, 0, 4)$ is

Options :

1. ✗ $x - 2z + 7 = 0$

2. ✗ $x + 2z - 9 = 0$

3. ✗ $x + 2y - 2z + 7 = 0$

4. ✓ $x + 2y + 4z - 17 = 0$

Question Number : 97 Question Id : 59425311126 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The maximum number of common tangent planes to the spheres $x^2 + y^2 + z^2 = 1$, $(x - 10)^2 + (y - 20)^2 + (z - 30)^2 = 1$ is

Options :

1. ✗ 1

2. ✗ 2

3. ✘ 3

4. ✔ 4

Question Number : 98 Question Id : 59425311127 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The equation $2xy + 4yz + 7xz = 0$ represents a

Options :

1. ✘ sphere

2. ✘ pair of straight lines

3. ✘ cone

4. ✔ cylinder

Question Number : 99 Question Id : 59425311128 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The angle between the planes $2x - y + z = 6$ and $x + y + 2z = 7$ is

Options :

1. ✘ $\cos^{-1}\left(\frac{4}{\sqrt{21}}\right)$

2. ✘ $\frac{\pi}{3}$

3. ✔ $\frac{\pi}{6}$

4. ✘ $\frac{\pi}{2}$

Question Number : 100 Question Id : 59425311129 Question Type : MCQ Option Shuffling : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0.25

The equation of the line joining the points $(-2, 4, 2)$ and $(7, -2, 5)$ is

Options :

1. ✔ $\frac{x}{-1} = \frac{y}{2} = \frac{z}{1}$

2. ✘ $\frac{x+2}{7} = \frac{y+4}{-2} = \frac{z+2}{5}$

3. ✘ $\frac{x+7}{3} = \frac{y-2}{2} = \frac{z+5}{1}$

4. ✘ $\frac{x+2}{3} = \frac{y-4}{-2} = \frac{z-2}{1}$